Robust Identification of Concealed Dangerous Substances by Spectral Correlation of Terahertz Transmission Images

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Abstract—Terahertz images containing spectral information in each pixel are recorded in transmission mode using a fiber-coupled time-domain spectroscopy system. The images are acquired by mounting a sample holder on an x-y stage, which is stepped across the beam in the two transverse directions, while the transmitted THz waveform is captured. The materials under investigation consist of uncovered and hidden samples of an explosive (RDX) and simulants (lactose and tartaric acid). Spectral angle mapping is used to identify the materials in the Terahertz images by comparing the spectrum in each pixel with a library of reference spectra for the different materials. We test the performance of several spectral characteristics derived from the measured transmission spectra. Robustness is studied by investigating the Receiver-Operating-Characteristics (ROCs). The ROCs are used to find which of the spectral characteristics is most robust to different sample preparation conditions, without the need for extensive pre-treatment of the data, such as baseline correction. Simple theoretical considerations are used to support the experimental results.

Index Terms—Terahertz, spectroscopy, imaging.

I. INTRODUCTION

ONE of the most promising applications of Terahertz spectroscopy is detection and identification of dangerous and/or illegal substances [1]. The ability to penetrate common materials, such as plastics, cloth, and cardboard, allows for identification of these substances, even when they are concealed. We here investigate the robustness of a simple spectral recognition method known as spectral angle mapping (SAM) [2]. In SAM the measured spectral characteristic of each pixel in the THz image is compared with a library of spectral characteristics by representing the characteristic as a vector and calculating the dot product, yielding the spectral correlation. We test several characteristics derived from the measured transmission spectra. Robustness is studied by investigating the Receiver-Operating-Characteristics (ROCs). The ROCs are generated by sweeping the identification (spectral correlation) threshold from −1 to 1 and counting the fraction of true-positive and false-positive pixels in the THz image. Preliminary results of this work have previously been presented in Ref. [3].

The combination of imaging and spectroscopy in security applications has the advantage of both being able to detect objects with a suspected shape as well identifying possibly harmful or illegal substances. THz imaging and a number of applications are reviewed in Ref. [4]. In this work the imaging capability is used to gather many spectra of the targets and the emphasis is on the spectral analysis. The object recognition is left to image processors at this stage. The issue of spectral identification is not new and has been used in for instance far-infrared Fourier transform (FTIR) spectroscopy. Localizing an absorption peak is relatively straight forward when the line is narrow, a common situation for FTIR spectra of gases. THz spectra of common simulants and explosives have rather broad peaks making it harder to pin down peak locations and hence identify substances. The literature on THz spectroscopy is growing, a selection of references are listed in Refs. [5]–[18]. The identification process is generally a question of matching a library spectrum to a measured spectrum and detection is declared if, in some metric, a threshold is exceeded. As a first cut at viewing the identification process one can look at it as a two-dimensional space with the different metrics (ways to compare spectra) along one axis and the spectral characteristics (which processed form of the raw spectrum) along the second axis. Common methods include principal component analysis (PCA) and spectral angle mapping (SAM) [5], [7], [9], [14], although also other methods have been used [12]. As to what to compare, there are several options, the raw spectrum, the raw spectrum normalized by a reference spectrum (transmission coefficient), and the absorbance. In addition, some groups apply preprocessing to their spectrum: removing water vapor lines and background scattering. Some authors pointed out that application of THz spectroscopy to security issues is not without difficulties [16]–[18]. It is the aim of this paper to quantify the spectral identification process by comparing several approaches and studying their false alarm rates.

In this work we have made several choices. (i) As a metric we chose SAM because of its simplicity and its intuitive nature. No extensive training of the algorithm is required, only a single library spectrum suffices. (ii) Preprocessing is limited to windowing of the time-domain signals. Water vapor lines and background scattering are not removed to allow for more realistic performance comparison. (iii) The different approaches are compared by studying their receiver operating characteristics (ROC), a simple visualization of their performance.

II. THEORY

We will here describe how spectral angle mapping can be used to identify materials based on measured terahertz
transmission spectra. From the scalar product of two vectors, \( \mathbf{a} \) and \( \mathbf{b} \), one can determine the cosine of the angle between them, according to the relation

\[
\cos \theta = \frac{\mathbf{a} \cdot \mathbf{b}}{ab}
\]  

(1)

Similarly, from two spectral vectors, \( \mathbf{S} \) and \( \mathbf{S}_r \), one can form new spectral characteristics, \( \mathbf{K}(\mathbf{S}) \) and \( \mathbf{K}(\mathbf{S}_r) \), where \( \mathbf{K} \) is a vector function of the spectrum, and use the scalar product to find the cosine of the angle between them, which we denote as the spectral correlation; a number between \(-1\) and \(1\), where \(1\) means perfect correlation. In this way one can compare a measured spectrum with a reference spectrum. The typical range of values of the spectral correlation depends strongly on which spectral characteristic \( \mathbf{K} \) is used. However, a good spectral characteristic should yield a spectral correlation close to zero for two uncorrelated spectra and close to one for two similar spectra. It is thus important to choose a suitable spectral characteristic for optimal identification of the materials. The following expressions for \( \mathbf{K} \) are tested and compared here:

- \( \mathbf{K}_1 = \mathbf{S} \), where \( \mathbf{S} \) is the raw spectrum (spectral amplitude).
- \( \mathbf{K}_2 = -\ln \mathbf{T} \), where \( T(f_i) = \frac{S(f_i)}{S_{\text{air}}(f_i)} \) and \( S_{\text{air}} \) is the spectrum of a measurement without sample, and \( f \) is the frequency.
- \( \mathbf{K}_3 = -\frac{\ln T}{d f} \).

To estimate the performance of the spectral characteristics above, we consider the case where a sample is covered by a barrier material. As a simple approximation, we assume that the measured THz transmission spectrum is given by

\[
S(f_i) = S_{\text{air}}(f_i)T_0 \exp \left[-\alpha(f_i)L\right],
\]  

(2)

where \( T_0 \) is a constant attenuation factor, \( \alpha \) is the absorption coefficient of the sample, and \( L \) is the sample thickness. The constant factor \( T_0 \) includes transmission through the barrier, as well as Fresnel reflection losses at the surfaces of the sample. A constant \( T_0 \) gives rise to a baseline in the absorbance \( \mathbf{K}_2 \). In Eq. (2), we have neglected multiple reflections from the sample and barrier materials, spectral characteristics of the barrier material, scattering from sample and barrier inhomogeneities, and noise.

From Eqs. (1)–(2) one can show that \( \mathbf{K}_1 \) gives a spectral correlation which is independent of a constant attenuation \( T_0 \) of the THz signal, but the spectral correlation is dependent on sample thickness. \( \mathbf{K}_2 \) gives the same spectral correlation for samples consisting of identical materials, with different sample thickness, as long as \( T_0 = 1 \). \( \mathbf{K}_3 \) gives the same spectral correlation for samples consisting of identical materials, with different sample thickness, for any constant value of \( T_0 \). For example, using Eq. (2), we obtain \( \mathbf{T} = T_0 \exp (-\alpha L) \) giving \( \mathbf{K}_3 = \frac{\alpha}{d f} L \). Thus

\[
\frac{\mathbf{K}_3}{\mathbf{K}_3} = \frac{\frac{\alpha}{d f}}{\sqrt{\int \left(\frac{\alpha}{d f}\right)^2 df}} = \frac{\alpha}{\sqrt{\alpha^2}},
\]  

(3)

which is independent of \( L \) and \( T_0 \). The last point is especially important, as it avoids the need of baseline removal, as long as the baseline is frequency independent. A spectrally varying baseline, for example due to scattering, will have a negligible effect on spectral correlations based on \( \mathbf{K}_3 \), as long as the variation is sufficiently slow. Thus, based on these arguments, \( \mathbf{K}_3 \) is most robust to variations in measurement conditions.

To illustrate these considerations we generated an example spectrum with a single absorption line, the black curve in Fig. 1, and call this our library spectrum. The effect of a constant attenuation, possibly due to a concealing material, is modeled by the blue curve in the same figure. A thicker sample or a higher-concentration sample would yield a stronger absorption, represented by the red curve. To test the specificity of the THz signal, but the spectral correlation is dependent on this characteristic is to be used to identify substances. This characteristic is not sensitive (red - 1.00) to variations in absorption lines, as well as their correlation with the library absorbance. See Fig. 1 for further explanation.
in sample thickness (absorption strength) and shows some specificity (green - 0.78).

Finally, consider the derivative of the absorbance. The curves are plotted in Fig. 3. This characteristic is neither sensitive to a constant attenuation nor to varying absorption strength: the correlation with the original spectrum is still perfect. In fact, it can be shown that even a slowly varying (polynomial of low order) background attenuation does not significantly hamper identification. In addition, this characteristic shows good specificity: the correlation for the model with the displaced absorption peak is significantly reduced (green - 0.39).

Based on this analysis the derivative of the absorbance appears to be the most promising spectral characteristic for identifying unknown spectra: it is both less sensitive to measurement conditions and more specific than the other characteristics.

III. SETUP

The THz setup is based on a fiber-coupled time-domain spectroscopy system pumped by 100-fs pulses at 780 nm wavelength from a frequency-doubled Er-doped fiber laser [19]. THz images are acquired by mounting a sample holder on an \( x-y \) stage, which is scanned through the beam, with step size 1 mm, while the transmitted THz waveform is captured. In this way a THz spectrum (after Fourier transform) is acquired for each stage position (pixel). A schematic of the setup is shown in Fig. 4. The distance between the emitter and detector modules is 31 cm and the sample holder has room for \( 3 \times 3 \) sample pellets, with diameter 32 mm and thickness up to 4.2 mm. Fig. 4 (inset) shows the labeling of the sample positions. Teflon (25 \( \mu \)m average particle size) was used as a binder material, which was mixed with tartaric acid, lactose, or RDX and then pressed into pellets using a 2 ton press in two minutes. The bottom row of the sample holder (position 7–9) was used for reference measurements, using a metal plate (position 7), no sample (position 8), and a pure Teflon sample (4 mm thickness, position 9). All measurements were performed in ambient air (21–26\(^\circ\)C, 10–50% relative humidity). The signal at each position of the \( x-y \) stage (pixel) was measured with a time window of 60 ps and a scan speed of 1 ps/s, with a sample rate of 32 Hz.

Figure 5(a) shows reference spectra for an open beam (air) and blocked beam (noise). An example spectrum for a 10% (mass percent) RDX sample, with 3.5 mm thickness, is also shown in the figure. All spectra were calculated from the time-domain signals by first applying a Blackman-Harris window with 30 ps half-width, centered in time at the signal peak, and then calculating the Fourier transform (FFT). The reference spectra indicate a bandwidth of \( \sim 2.5 \) THz and a peak signal-to-noise ratio (SNR) of \( \sim 60 \) dB. Figure 5(b) shows the absorbance \( (K_x) \) for samples containing RDX (10%, 3.5 mm thickness), tartaric acid (10%, 4.0 mm thickness), and lactose (10%, 4.2 mm thickness). These samples were
used as reference samples in the spectral library. The part of
the spectrum spanning the frequency range 0.1 to 1.3 THz
was used in the correlation calculations, as the SNR is high
in this frequency range (SNR > 40 dB for an open beam).
Although there are several water vapor absorption lines in
this wavelength range [15], we did not perform any numerical
removal of water lines in the data processing. The location
of the water lines was used to verify the calibration of the
frequency axis in our measurements. Also shown in Fig. 5(b)
is the absorbance of the cloth barrier used in some of the
experiments.

IV. RESULTS

THz transmission measurements were carried out for sam-
pies containing tartaric acid, RDX, and lactose, and mixtures
of two of these substances.

A. Uncovered samples

<table>
<thead>
<tr>
<th>Sample no.</th>
<th>Tartaric acid mass fraction</th>
<th>Total mass (g)</th>
<th>Thickness (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5%</td>
<td>6.1</td>
<td>3.9</td>
</tr>
<tr>
<td>2</td>
<td>2%</td>
<td>6.3</td>
<td>4.0</td>
</tr>
<tr>
<td>3</td>
<td>1%</td>
<td>6.1</td>
<td>3.9</td>
</tr>
<tr>
<td>4</td>
<td>10%</td>
<td>3.1</td>
<td>2.3</td>
</tr>
<tr>
<td>5</td>
<td>10%</td>
<td>1.5</td>
<td>1.2</td>
</tr>
<tr>
<td>6</td>
<td>5% (unground)</td>
<td>6.2</td>
<td>4.0</td>
</tr>
</tbody>
</table>

Six tartaric acid samples were placed in the two top rows
of the sample holder. The tartaric acid mass percent and sample
thickness is shown in Table I. Sample no. 6 consisted of
unground tartaric acid, while the tartaric acid was ground for
the others. A reference spectrum for tartaric acid was measured
using a 10% tartaric acid sample with 4 mm thickness, and is
shown in Fig. 5(b).

Based on the measured terahertz transmission spectral im-
age, a spectral correlation between each pixel and the reference
sample was calculated. This assigns, in theory, a value between
-1 and 1 to each pixel. Usually, amplitude or power spectra
have only positive values for each frequency and SAM will
then only yield correlation values ≥ 0. Derivatives of spectra
may have negative values and negative correlation values are
possible. All pixels containing tartaric acid (i.e. the same
material as the reference sample) are labeled positive pixels,
the remaining pixels being negative. One can classify a pixel
by comparing its correlation value with a certain threshold.
If the correlation value is larger than the threshold and the
pixel is positive, the outcome is denoted as true positive. If,
on the other hand, the correlation value is larger than the
threshold and the pixel is negative, the outcome is denoted
as false positive. The true positive rate (TPR) is the number
of true positive pixels divided by the number of positive
pixels and the false positive rate (FPR) is the number of
false positive pixels divided by the number of false pixels.
By stepping the threshold from −1 to 1 and calculating the
TPR and FPR for the pixels in the image, we obtain the
ROC curves in Fig. 6(a). The ROC curves are based on
the three spectral characteristics described in Sec. II. We
observe from the ROC curves that the spectral characteristic
$K_3$ gives significantly better performance, compared to more
common characteristics, such as the raw spectrum, $K_1$, and
the absorption spectrum, $K_2$.

In practice, it will usually be desirable to operate in a
regime where the fraction of false positive pixels is very low,
while the fraction of true positive pixels is high, corresponding
to the upper left corner of the ROC curves. The spectral
correlation value corresponding to the upper left corner of the
ROC curves is found by identifying the correlation threshold
which give the largest difference between the fraction of true
positive and false positive pixels (TPR – FPR). The results of
this calculation are shown in Fig. 6(b). We observe from

![Fig. 6. Testing for tartaric acid, uncovered samples. (a) ROC curves for
the three spectral characteristics for a THz image (transmission mode) of six
samples containing tartaric acid, RDX, and lactose, and mixtures of two of
these substances. (b) Identifying the optimal identification threshold. (c) A
spectral correlation image using the spectral characteristic $K_3$.](a) (b) (c)
the figure that the optimum correlation threshold is about 0.25 for the spectral characteristics $K_2$ and $K_3$, while a much higher correlation threshold of about 0.85 is optimal for the spectral characteristic $S$. We also note that the blue curve in Fig. 6(b), corresponding to the $K_3$ characteristic, is broader, suggesting less sensitivity to the choice of the actual threshold value than for the other characteristics considered here. Figure 6(c) plots the correlation value in each pixel using the best spectral characteristic, $K_3$. We observe from the figure that the correlation is somewhat lower for the (1%, 4 mm) sample (position 3) and for the sample containing unground tartaric acid (position 6), compared to the other tartaric acid samples. This is not unexpected, because a low tartaric acid fraction (position 3) leads to noisier absorption peaks, while unground tartaric acid (position 6) leads to more scattering.

B. Covered samples

TABLE II

<table>
<thead>
<tr>
<th>Sample no.</th>
<th>Mass fraction</th>
<th>Total mass (g)</th>
<th>Thickness (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10% tart. acid</td>
<td>6.1</td>
<td>4.0</td>
</tr>
<tr>
<td>2</td>
<td>10% lactose</td>
<td>6.4</td>
<td>4.2</td>
</tr>
<tr>
<td>3</td>
<td>10% RDX</td>
<td>5.5</td>
<td>3.5</td>
</tr>
<tr>
<td>4</td>
<td>5% tart. acid, 5% lactose</td>
<td>6.5</td>
<td>4.2</td>
</tr>
<tr>
<td>5</td>
<td>5% RDX, 5% tart. acid</td>
<td>5.7</td>
<td>3.5</td>
</tr>
<tr>
<td>6</td>
<td>5% RDX, 5% lactose</td>
<td>5.8</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Measurements of samples covered by a barrier consisting of one layer of 1.0 mm-thick cloth were also carried out. The samples in this case contained RDX, lactose, and tartaric acid, and mixtures of two of these substances, as shown in Table II. The absorbance of the reference samples for the spectral correlation calculations are shown in Fig. 5(b), together with the absorbance of the cloth barrier.

Figure 7 shows application of SAM to identify the samples containing RDX. Similarly to the case with uncovered samples, we generate ROC curves for the different spectral characteristics. The results are shown in Fig. 7(a). We observe that in the limit of low false positive rate, the spectral characteristic $K_3$ is superior to the two other characteristics, which was also the result for the measurements on the uncovered tartaric acid samples in Sec. IV-A. Figure 7(b) shows that the optimal correlation thresholds are different, compared to Fig. 6, for all three spectral characteristics. For the spectral characteristic $K_3$ a correlation threshold of about 0.35 is optimal in this case. The observation that the optimal correlation threshold depends on measurement conditions means that one must either use a low correlation threshold to ensure that the fraction of true positive pixels is high, at the expense of increased false positive rate, or must use a high correlation threshold to ensure that the false positive rate remains low, at the expense of decreased true positive rate. Which of the two strategies is optimal depends on the application. Figure 7(c) shows a spectral correlation image produced using the metric $K_3$. The structure of the cloth appears as the wavy horizontal lines in the image. The three samples containing RDX distinguish themselves from the other samples suggesting both good detectivity and specificity. Clearly, the sample containing RDX only is best identified, followed by the one mixed with lactose. The sample mixed with tartaric acid correlates a bit less with the "pure" RDX spectrum. Looking at Fig. 5(b) we observe that the spectral features of RDX and lactose are better separated than the ones of RDX and tartaric acid. This may explain the observed differences in correlation: the RDX spectrum is less disturbed by the lactose than by the tartaric acid.

Figure 8 shows application of SAM to identify tartaric acid for the covered samples. The figure is based on the same experimental data as in Fig. 7, but the reference spectrum is tartaric acid, instead of RDX. From Fig. 8, we note several points. First, the optimal correlation threshold is lower (about...
In conclusion, we have used ROC curves to compare three potential spectral characteristics for use in spectral angle mapping. By measuring on covered and uncovered samples of varying thickness, consisting of pure and mixed materials, we identify the first derivative of the absorption spectrum as a better overall metric, compared to the absorption spectrum or the raw transmission spectrum, although the absorption spectrum shows comparable performance for some combinations of samples and barriers. Furthermore, only a single reference spectrum is needed for each material in the spectral database. This approach might find uses within application of THz transmission spectroscopy for identification of dangerous or illegal substances, for example by assisting a human operator in the interpretation of THz transmission images.

REFERENCES


**Arthur D. van Rheenen** obtained his PhD in Electrical Engineering (1987) from the University of Florida, Gainesville. From 1980 to 2005 he has published on different aspects of noise in electronic devices. The last 10 years he has been studying and modeling propagation or IR radiation through the atmosphere. In addition, imaging and spectral recognition of dangerous and/or illegal substances using THz technology has been a research theme over the last five years.

**Magnus W. Haakestad** received a PhD in electrical engineering from the Norwegian University of Science and Technology in 2006. Since then he has been a scientist at the Norwegian Defence Research Establishment. His research interests include infrared laser sources, nonlinear optics, fiber optics, and terahertz technology. He spent one sabbatical year at Edward L. Ginzton Laboratory, Stanford University, where he worked with mid-infrared frequency combs for molecular spectroscopy.